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PLA C YIELDING OF PARTIALLY-CRYSTALLINE POLYMERS

by

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molecular model of the yielding process in which polymer chains, folded to different degrees in the crystallites, are pulled taut. Values of yield and draw stress were found to be of the same order as the free energy  $U_m^{\pi}$  of melting, suggesting that yielding and drawing take place by stress-induced disruption of crystallites, analogous to melting. The mechanical work of drawing was similar to, but generally larger than, that required for melting, ranging from  $U_m^{\pi}$  to about  $4U_m^{\pi}$ . The difference is attributed to strain energy of drawn material and possible recrystallization during drawing.

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## 1. Introduction

Although much is known about the microstructure of semi-crystalline polymers, there is surprisingly little published work dealing with their physical properties in a quantitative way. As pointed out previously (1), they show remarkable differences in ductility. High-density polyethylene has a natural draw ratio of about 10X whereas trans-polyisoprene has a natural draw ratio of only about 3X. Other examples are given below. These differences do not seem to be due solely to differences in crystallinity. Indeed, the more crystalline materials appear to have generally higher natural draw ratios, contrary to expectation. It has been suggested, instead, that the extensibility of crystalline polymers is related to the degree of molecular chain folding within the crystallites; highly-folded chains being capable, at least in principle, of large extensions (1,2).

A second important property of crystalline plastics is their yield stress, i.e., the maximum stress that they can withstand before the onset of general plastic deformation. Again, although different polymers show markedly different yield stresses, there does not appear to be a generally-accepted connection between the microstructure and resistance to yielding. Some comparative measurements of yield and draw stresses have therefore been made for a number of common semi-crystalline plastics, over a broad temperature range. They are reported here, and compared with predictions of a simple theoretical model, in which drawing is attributed to stress-induced "melting". The principal factors affecting the yield and draw stresses are thus

the degree of crystallinity and the free energy of melting.

A similar hypothesis was put forward by Guska and Harrison (3,4). They focussed attention on the maximum elastic strain energy that the material can support before yielding, and implied that it is correlated with the heat of fusion, but they did not propose a quantitative relationship between the two parameters. Popii and Mandelkern (5) also summarized evidence in favor of stress-induced melting, at least in part, as a mechanism of plastic yielding in polyethylene, but again did not propose a quantitative relationship.

Hartman, Lee and Cole suggested a strain energy criterion for yielding in semi-crystalline polymers, principally to account for the temperature dependence (6). However, their treatment does not deal with the mechanism of deformation considered here, by disrupting crystallites.

Glassy polymers also yield, in a superficially similar way, but on a smaller scale, confined to narrow shear bands or to microscopic crazes, and at considerably higher stresses. A broadly-similar hypothesis to that put forward here for plastic yielding and drawing in crystalline polymers was proposed previously to account for the phenomenon of crazing (7). A stress-induced transition from the glassy state to a rubbery or liquid state was shown to account for several aspects of crazing; notably, the relation between strength and molecular weight (8), and "environmental stress cracking", i.e. the tendency of certain fluids that are rather poor solvents for the polymer to lower the stress level at which crazes appear (7). We now examine the hypothesis of a stress-induced phase

transition, i.e., melting, as the mechanism of ductile deformation of semi-crystalline polymers above their glass transition temperatures.

## 2. Experimental details

Several semi-crystalline polymers were employed in this study : high and low density polyethylene (HDPE and LDPE), polypropylene (PP), polycaprolactone (PCL), polybutene-1 (PB), trans-polyisoprene (TPI), lightly-crosslinked trans-polychloroprene (TPC), and polytetrafluoroethylene (PTFE). Details of the materials are given in the Appendix.

In each case the polymer was molded as a sheet, about 0.8 mm thick, in a hot press at a temperature above the melting temperature for a period of about one hour. The molded sheet was then cooled rapidly to room temperature, about 20°C.

Dog-bone-shaped samples, having a parallel-sided central portion about 20 mm long and 2 mm wide, were cut from the molded sheets. They were stretched at various rates in a tensile test machine, at temperatures between -40°C and 160°C . A schematic relation between tensile force and displacement of the ends of the sample is shown in Figure 1 ,with sketches of the sample at different stages of deformation.

Several physical properties were determined from the experimentally-determined stress-strain relations: the yield stress  $\sigma_y$  at which the tensile force passed through a maximum, the draw stress  $\sigma_d$  , sometimes appreciably lower than the yield stress, the natural draw ratio  $\Delta_d$ , i.e., the constant extension ratio in the drawn part of

the sample as the neck propagated, transforming undrawn material into the drawn state, and the breaking stress, denoted  $\sigma_b$ . Results obtained at room temperature are given in Table 1. In all cases, stresses refer to the original (unstrained) cross-sectional area of the sample.

Estimates of the degree of crystallinity  $c$  of each sample were obtained from measurements of the heat of fusion by DSC, using reported values of the heat of fusion  $h$  of 100 percent crystalline material. They are included in Table 1.

### 3. Experimental results and discussion

#### (i) Nature of plastic yielding in crystalline polymers

Although the general pattern of plastic yielding has been described many times, some features do not seem to have been pointed out previously. The characteristic neck first appears at an angle  $\beta$  of about  $55^\circ$  to the direction of tension, rather than at  $90^\circ$ , as shown in Figure 2a. This feature was particularly clear in harder materials such as HDPE, PP, PCL, and TPI. It is in good agreement with the criterion,  $\cos 2\beta = -1/3$ , given by Bowden (9) for neck formation without change in one dimension, a condition imposed by the rigidity of the still unyielded material on either side of the nascent neck. Then, as the neck propagates, the constraint imposed by neighboring material diminishes and the angle  $\beta$  changes to  $90^\circ$ , Figure 2b.

In TPI, propagation of the neck could be seen to take place intermittently, by periodic movement of a band of material from the undrawn part into the drawn part, forming characteristic striations, Figure 3. This process continued from the initial formation of a neck until drawing was complete. It indicates that the drawing process is not homogeneous but involves discrete portions of material, taken successively to the fully-drawn state.

Similar details of the drawing process were not observable in other polymers, like LDPE, which formed a neck more gradually, and at significantly larger strains (5). Indeed, at low rates of strain, below about  $1 \times 10^{-3} \text{ s}^{-1}$ , TPC, PB, and LDPE extended more or less uniformly, without forming a visible neck.



## (ii) Physical properties

Striking differences were found in the physical properties of the different polymers, as shown by the results given in Table 1. Values of the natural draw ratio  $\lambda_d$  ranged from 2 to 10. Yield stresses ranged from 7 to 21 MPa at room temperature, and draw stresses varied similarly, lying somewhat below the yield stress.

As the test temperature was varied, the draw ratio was found to remain substantially unchanged but the yield and draw stresses decreased sharply with increasing temperature. Typical relations are shown in Figures 4 and 5. For several materials, the dependence was approximately a linear one, Figure 4, and the yield and draw stresses fell to zero at the melting temperature of the sample, somewhat below the thermodynamic melting temperature, given in Table 1. For PP, HDPE, LDPE and PTFE, the yield and draw stresses followed a non-linear dependence on temperature, as shown in Figure 5, but they still fell to zero at a temperature, obtained by extrapolation, close to the melting temperature. We now turn to the physical interpretation of these results.

## (iii) Natural draw ratio, breaking extension, and recovery from the drawn state

Employing the concept put forward previously, that drawing takes place by straightening crystalline and amorphous molecular sequences, the observed values of natural draw ratio  $\lambda_d$  can be interpreted in terms of the number  $\bar{f}$  of times that a molecule passes through the same crystallite (1):

$$1/\lambda_d = (c/\bar{f}) + (1 - c)^{1/2}/\bar{n}^{1/2}. \quad (1)$$

where  $\bar{n}$  denotes the number of equivalent random links between points

molecular entanglement in the melt, typically between 100 and 300. Values of  $f$  were calculated in this way from the measured natural draw ratios. They were approximately 1 for TPI, TPC, and PE, indicating little or no re-entry into the same crystallite, and 2 to 4 for LDPE, PTFE, PP, and PCL, indicating a limited amount of molecular reversal and re-entry. For HDPE the value of  $f$  was relatively large, about 11, suggesting that a substantial degree of chain folding occurred in this case. But it is noteworthy that HDPE was quite unusual in this respect, reflecting an unusually high natural draw ratio (10).

After reaching the fully-drawn state, samples could then be extended further, now homogeneously, until the breaking stress and strain were reached. The extension at break was found to be generally about twice as large as the extension attained in drawing. Thus, HDPE, which had a natural draw ratio of about 10X, finally broke at a tensile strain of about 18, and PCL, which drew by a factor of 5X, broke at an extension of about 10.

It is clear that substantial further rearrangement of crystalline and amorphous material can take place after the natural draw ratio has been reached. Previously it was proposed that the natural draw ratio is that deformation at which molecules that happen to traverse a crystallite unfavorably, with their entangled junctions at opposite sides and lying in the direction of the applied tension, become fully stretched (1). Other molecules, more favorably situated, will reach the fully-stretched state later. Thus, extensive molecular rearrangement after the natural draw ratio is reached, permitting further extension of drawn material, is not incompatible

with the proposed mechanism of drawing.

Measurements were also made of the retraction of drawn samples on heating. When the tension was released, the immediate recovery was quite small, less than 10 percent of the imposed extension. On warming, the samples began to retract, as shown in Figure 6, and recovery was virtually complete at the melting temperature.

There was one outstanding exception, however. Samples of PCL showed much less recovery, retaining more than one-half of the imposed strain at the melting point. This feature is tentatively attributed to unusually low molecular weight of the PCL sample, only about 40,000 g/mole. Extensive slippage of entangled molecules may well take place in this case during drawing. If this is so, then the inferred value of  $f$  for PCL, about 3, will be too high because the natural draw ratio has been over-estimated.

#### (iv) Theoretical interpretation of yield and draw stresses

We consider first the relationship between the draw stress and the thermodynamic work of melting,  $U_m$ , given by (11)

$$U_m = c \rho h (1 - T/T_m), \quad (2)$$

where  $c$  is the fractional degree of crystallinity,  $\rho$  is the density,  $h$  is the heat of fusion of 100 percent crystalline material,  $T$  is the test temperature and  $T_m$  is the crystal melting temperature. Values of these parameters are given in Table 1 for each polymer.

Experimental values of the draw stress  $\sigma_d$  are plotted in Figure 7 against calculated values of the work of melting  $U_m$ . The results are seen to fall into two groups: polymers with low values of natural draw ratio show rather good agreement between draw stress and the work

melting, whereas polymers with large natural draw ratios have much lower draw stresses, compared to the work of melting, only about one-fifth as large in the case of HDPE.

Similar conclusions are reached if yield stresses are considered instead of draw stresses. Values of yield stress  $\sigma_y$  are plotted against the thermodynamic work of melting in Figure 8. Again, polymers with low natural draw ratios, between 2 and 3, show satisfactory agreement between yield stress and the work of melting, whereas polymers having high ductility; for example, HDPE; have much lower yield stresses for equivalent values of  $U_m$ .

These differences between different polymers can be attributed to different energies of deformation, even for the same yield and draw stress. In the following section the work expended in drawing is compared to the free energy of melting. (A similar comparison is not made for yielding because the yield stress depends significantly upon the rate of stretching, as discussed later.)

Although significant differences are present, as pointed out above, surprisingly good numerical agreement is obtained between observed yield and draw stresses and the computed work of melting for a number of polymers. This empirical observation suggests that the hypothesis of Juska and Harrison is basically correct. However, it is thought that their estimate of the work required to bring about the melting transformation is inappropriate, as discussed below.

## (v) Work expended in plastic drawing

When plastic deformation occurs, energy is expended in drawing, given by the product of the draw stress and the extension accompanying drawing,

$$U = \sigma_d(\lambda_d - 1) . \quad (3)$$

It is proposed here that the criterion for drawing is that this mechanical work is enough to disrupt the crystallites completely, i.e.,  $U = U_m$ . This criterion differs somewhat from that proposed by Juska and Harrison (3,4), who employed the strain energy stored in the material at the onset of yielding as a measure of the work of melting.

Now, because several polymers have values of  $\lambda_d$  of the order of 2 to 3, the corresponding work of drawing will lie between  $\sigma_d$  and  $2\sigma_d$ , Equation 3. Thus, the degree of agreement found between the draw stress itself and the work of melting for these polymers is not so surprising. On the other hand, for PP, LDPE, and HDPE, with values of  $\lambda_d$  ranging between 4.5 and 10, the work of drawing  $U$  becomes a larger multiple of the draw stress and hence the draw stress itself will be a smaller fraction of the thermodynamic work of melting  $U_m$ , as is observed (Figures 7 and 8).

Approximate values of the effective draw strain  $\underline{e}_d^*$  can be deduced by comparing measured draw stresses with those predicted by Equations 2 and 3. They are listed in Table 2 and compared with the actual draw strains for each polymer. As can be seen, although the two values are of the same order, the effective draw strain and thus the work required to melt the polymer is generally lower than the work actually expended in drawing. In other words, the amount of mechanical work expended in drawing is similar to, but generally larger than that needed to melt crystalline material, by a factor between 1X and 4X.

Two possible reasons for this discrepancy can be put forward. Work of elastic deformation accompanying drawing has not been taken into account, although it is clearly present when drawn material is heated to the melting point and retracts to the unstrained state. And it is possible, at least for materials well below the melting point, that they recrystallize during drawing, before reaching the fully-drawn state. In this case, work of melting must be provided more than once during drawing. Unfortunately, neither of these effects are easily quantified. Either of them would cause the work of drawing to exceed the value calculated from Equations 2 and 3.

(vii) Effect of rate of deformation on yielding

It is helpful, again, to consider the polymers studied here in two groups. The first, those polymers having values of natural draw ratio between 2 and 3 showed very little dependence of the yield stress and draw stress on rate of deformation, Figures 9 and 10. Indeed, it should be noted that yield stresses and draw stresses were quite similar for these polymers.

The second group of polymers, having large values of natural draw ratio, showed a steady increase in yield stress with rate of deformation, Figure 9. At first sight, this dependence is inconsistent with the thermodynamic concept of stress-induced melting, taking place, in principle, at equilibrium. However, the work of deformation  $U$  employed here is obtained from drawing, and comparison is made of draw stress and draw ratio with theoretical predictions, rather than yield stress. And the draw stress was found to be less sensitive to rate of deformation, Figure 10. It is therefore

thought that a pronounced dependence of yield stress on rate of deformation does not vitiate the proposed mechanism of drawing by a stress-induced phase transition. But, clearly, further study is required of differences between yield stress  $\sigma_y$  and draw stress  $\sigma_d$ . They are particularly different for polymers with high natural draw ratios, stretched at high rates.

(vii) Polytetrafluoroethylene, PTFE

Yield and draw stresses for PTFE were remarkably low in comparison with estimated values of the work of melting, Figures 7 and 8. These results cannot be attributed to an excessively high degree of ductility for PTFE. On the contrary, the natural draw ratio was relatively low, about 3.3. Instead, it must be hypothesised either that the mechanism of yielding is distinctly different for PTFE, or, as seems more likely, that the effective melting temperature at which the structure flows under stress is much below the reported melting temperature. Intermediate melting transitions have been reported for PTFE (12,13).

#### 4. Conclusions

The following conclusions are obtained:

Several polymers, with low values of natural draw ratio, show good agreement between measured yield or draw stresses and those calculated from the work of melting. This empirical observation is regarded as good evidence for the basic Juska and Harrison hypothesis, that yielding is associated with stress-induced melting.

It is proposed that the work of drawing is primarily expended in meeting the thermodynamic requirements of melting. In accordance with this concept, the product  $\sigma_d \epsilon_d$  of the measured draw stress and natural draw strain is found to be of the same order as the free energy of melting. Numerical values range from 1X to 4X of the theoretical amount of work required to melt the material. Possible reasons for the discrepancy are that additional energy is expended in elastic deformation, and that recrystallization occurs during drawing.

Attention is focussed on draw stress and work of drawing, rather than yield stress and work of yielding. For polymers with low natural draw ratios, between 2 and 3, the distinction is unimportant because the yield stress and draw stress are quite similar. For polymers with higher natural draw ratios, notably low- and high-density polyethylenes, the yield stress is considerably higher than the draw stress, and more so at higher rates of deformation. Indeed, the dependence of the yield stress upon rate of straining, and upon time under load (14), suggests that it is not amenable to direct thermodynamic interpretation.



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Appendix

The following materials were used in the experiments.

High-density polyethylene (HDPE): Microsuntec R340P, from Asahi-

Kasei Ind., Japan. Density, 0.955 g/ml; melt index, 7 g/10 min.

Low-density polyethylene (LDPE): Flothene G801, from Asahi-

Kasei Ind., Japan. Density, 0.920 g/ml; melt index, 20 g/10 min.

Polypropylene (PP): PP 4092, from Exxon Chemical Company.

Density, 0.90 g/ml.

Polycaprolactone (PCL): PCL-700, from Union Carbide Corp. Density,

1.149 g/ml at 20°C; wt. av. mol. wt.,  $4 \times 10^4$  g/mole.

Polybutene-1 (PB): PB 8240, from Shell Chemicals.

Polytetrafluoroethylene (PTFE): Hoerst TFM 1600, from Pfaudler-

Edlon Products. Density, 2.17 g/ml.

Trans-polyisoprene (TPI): Trans-PIP 301, from Polysar Limited,  
Canada.

Trans-polychloroprene (TPC): Neoprene HC, from E. I. duPont de

Nemours and Co. This material was lightly crosslinked, using  
the following mix formulation, by heating for 1 h at 150°C.

Neoprene HC, 100; extra light calcined magnesia, 4; zinc

oxide, 5; Permalux (accelerator), 0.5; Antioxidant 2246, 1.

Table 1: Thermodynamic parameters and tensile properties at 25°C for eight semi-crystalline polymers.

Polymer	Heat of fusion $\underline{h}$ (kJ/kg)	Melting temperature $\underline{T_m}$ (°C)	Density $\underline{\rho}$ (g/ml)	Crystallinity $\underline{C}$ (%)	Draw ratio $\underline{\lambda_d}$	Yield stress $\underline{\sigma_y}$ (MPa)	Draw stress $\underline{\sigma_d}$ (MPa)	Stress at break $\underline{\sigma_b}$ (MPa)
HDPE	290	130	0.95	60	10.2	21	13	21
LDPE	290	120	0.917	31	4.5	9	9	10.5
PP	210	180	0.90	48	6.0	15a	11.5a	39a
PCL	136	70	1.15	59	5.3	18	13	38
PB	120	120	0.91	48	2.0	14	14	36
TPI	186	70	0.95	28	2.3	9	8	40
TPC	95	75	1.29	30	2.7	7	7	30.5
PTFE	63	335	2.17	67	3.3	13	12	37.5

<sup>a</sup>measured at 60°C.

Table 2: Comparison of measured draw strain  $\underline{e_d} (= \lambda_d - 1)$  with effective value  $\underline{e_d^*}$ , calculated from draw stress and work of melting, Equations 2 and 3.

<u>Polymer</u>	<u><math>e_d</math></u>	<u><math>e_d^*</math></u>
PB	1.0	1.0
TPI	1.3	0.9
TPC	1.7	0.9
PTFE	2.3	4.5
LDPE	3.5	2.5
PCL	4.3 <sup>a</sup>	1.0
PP	5.0	3.0
HDPE	9.2	3.0

<sup>a</sup>draw strain not fully recoverable, see text.

### Figure Legends

- Figure 1: Relation between tensile stress and mean elongation ratio, given by the overall length of the sample relative to its initial length.
- Figure 2: Formation and propagation of a neck in trans-polyisoprene (TPI).
- Figure 3: Striations in drawn trans-polyisoprene (TPI).
- Figure 4: Yield stress  $\sigma_y$  (open points) and draw stress  $\sigma_d$  (filled-in points) for PCL (O,●) and TPC (□,■), plotted against test temperature  $T$ . Rate of extension:  $\dot{\epsilon} = 0.015 \text{ s}^{-1}$
- Figure 5: Yield stress  $\sigma_y$  (open points) and draw stress  $\sigma_d$  (filled-in points) for HDPE (Δ,▲) and LDPE (▽,▼), plotted against test temperature  $T$ . Rate of extension:  $\dot{\epsilon} = 0.015 \text{ s}^{-1}$
- Figure 6: Residual strain  $\epsilon$  vs temperature for several polymers, drawn at 20°C to strains exceeding their natural draw strain and then released and heated.
- Figure 7: Draw stress  $\sigma_d$  vs free energy  $U_m$  of melting. ●, TPI; ○, PCL; ◆, PB; ■, TPC; X, PP; ▼, LDPE; ▲, HDPE; ►, PTFE. The broken line represents  $\sigma_d = U_m$ .
- Figure 8: Yield stress  $\sigma_y$  vs free energy  $U_m$  of melting. ○, TPI; ○, PCL; ◆, PB; □, TPC; +, PP; ▼, LDPE, Δ, HDPE. The broken line represents  $\sigma_y = U_m$ .

Figure 9: Yield stress  $\sigma_y$  at 25°C vs rate of extension  $\dot{\epsilon}$ .

+, PP;  $\Delta$ , HDPE; O, PCL;  $\diamond$ , PB;  $\triangleright$ , PTFE;  $\bigcirc$ , TPI;  $\square$ , TPC.

Figure 10. Draw stress  $\sigma_d$  at 25°C vs rate of extension  $\dot{\epsilon}$ .

X, PP;  $\blacktriangle$ , HDPE;  $\bullet$ , PCL;  $\blacklozenge$ , PB;  $\blacktriangleright$ , PTFE;  $\bullet$ , TPI;  $\blacksquare$ , TPC.

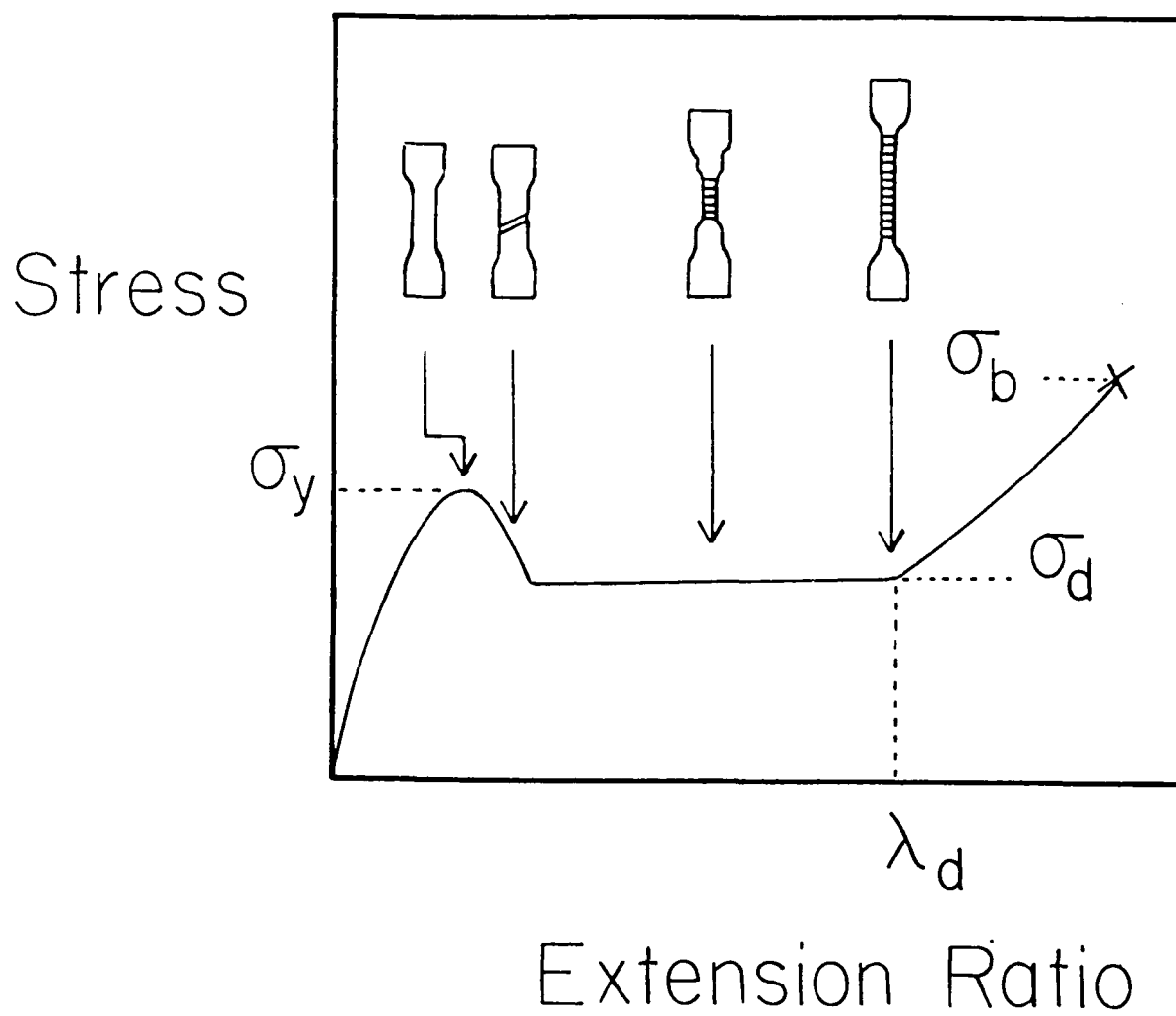
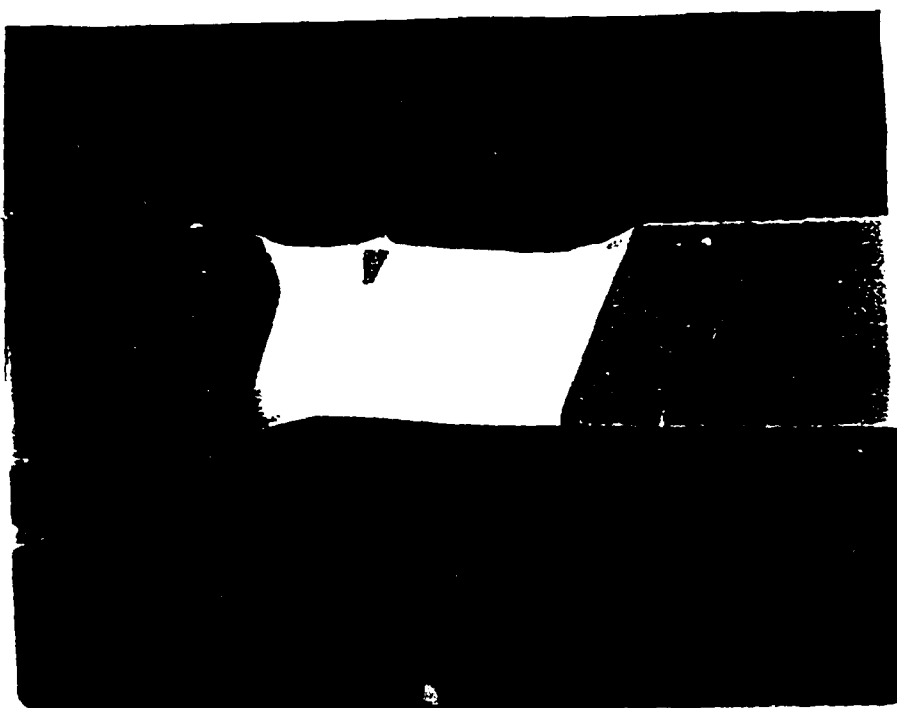
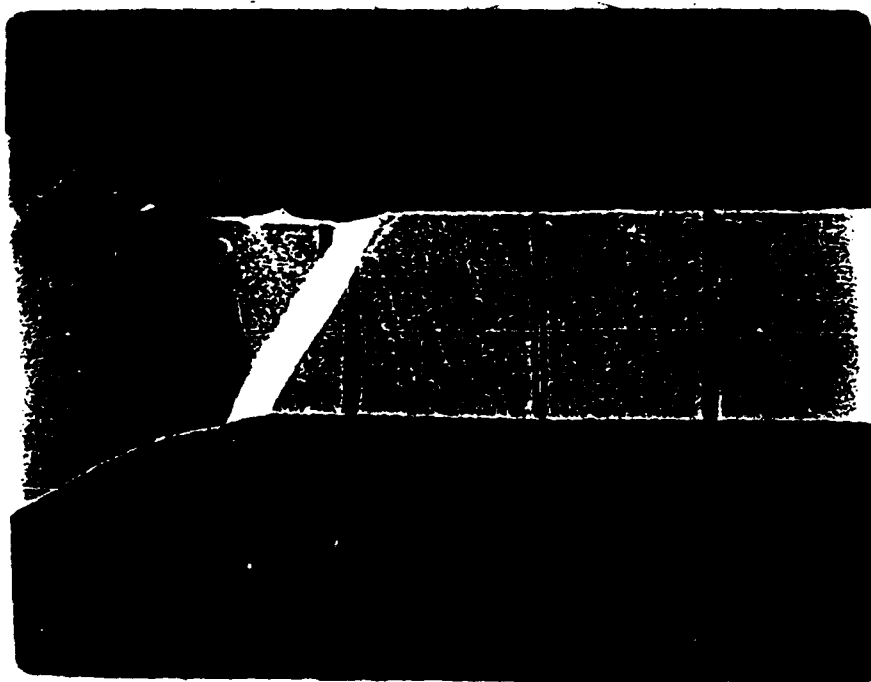


Figure 1





(b)



(a)

Figure 2

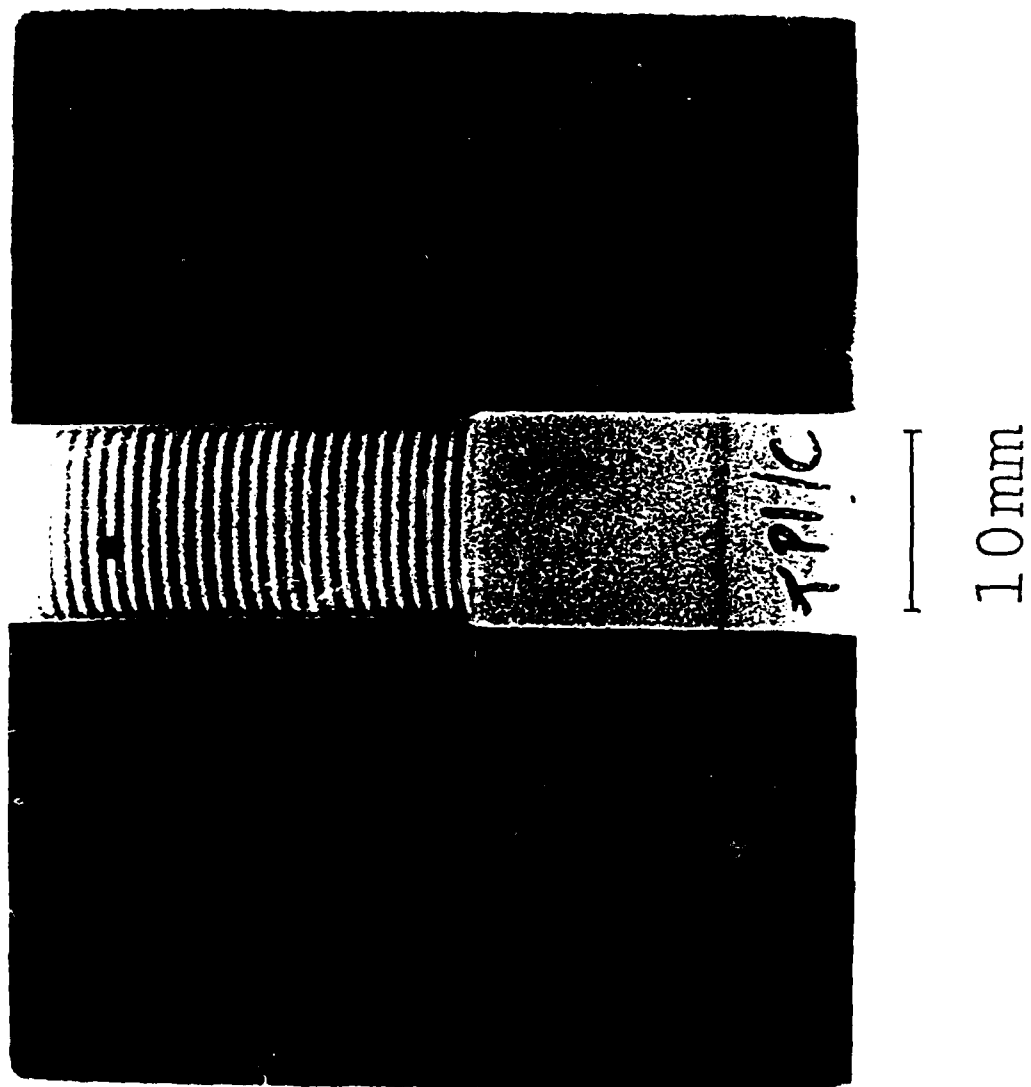


Figure 3

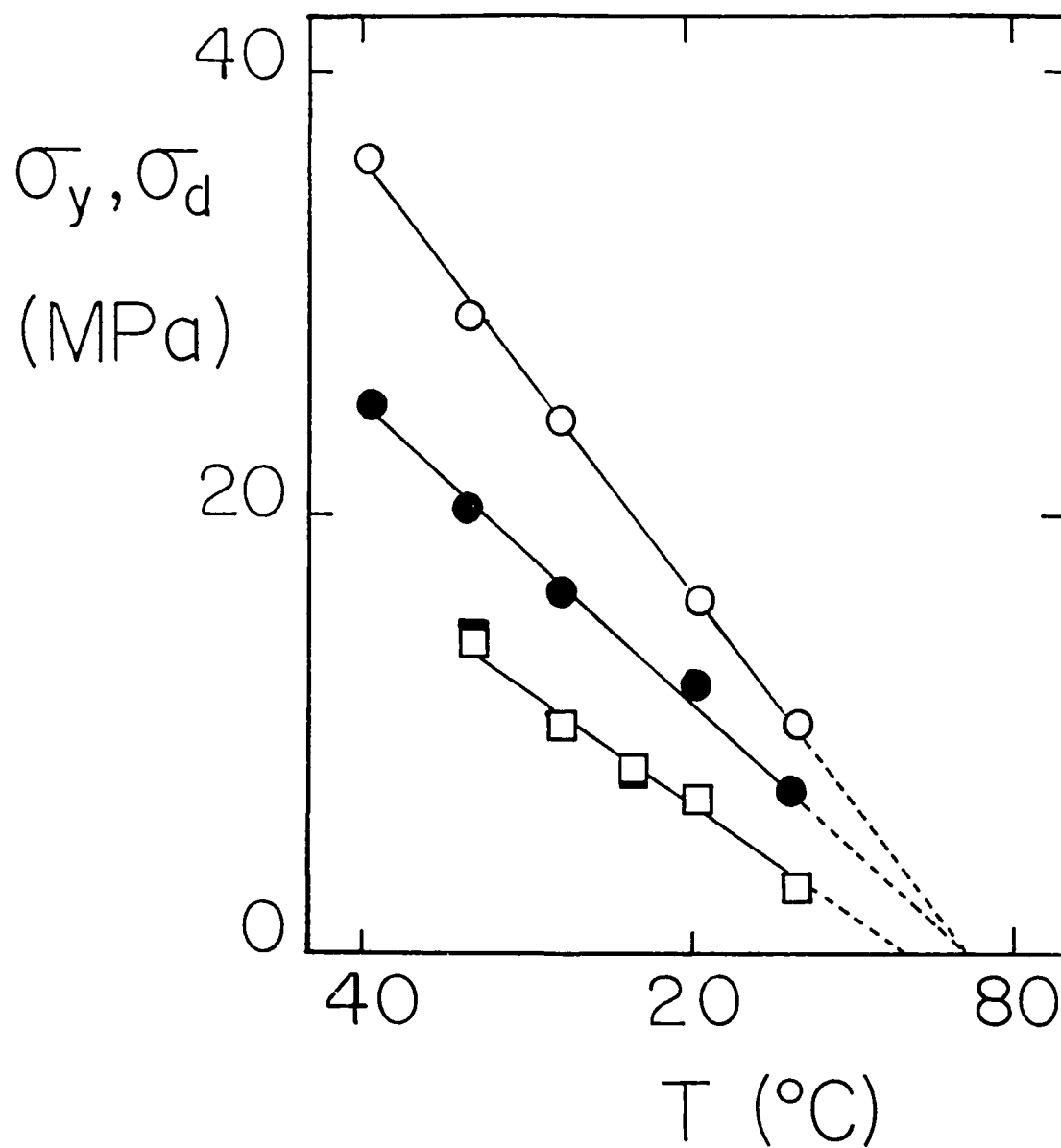


Figure 4

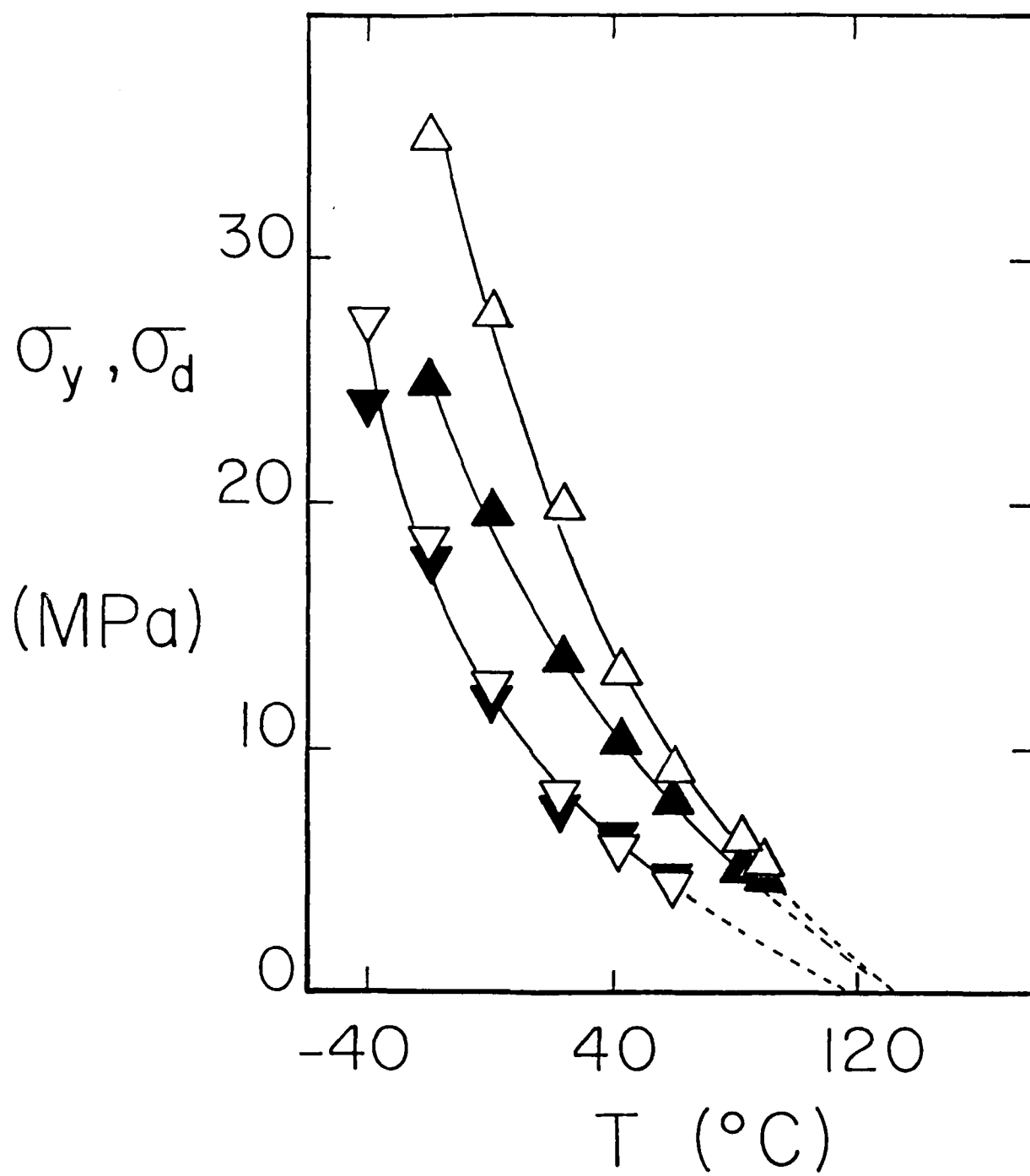


Figure 5

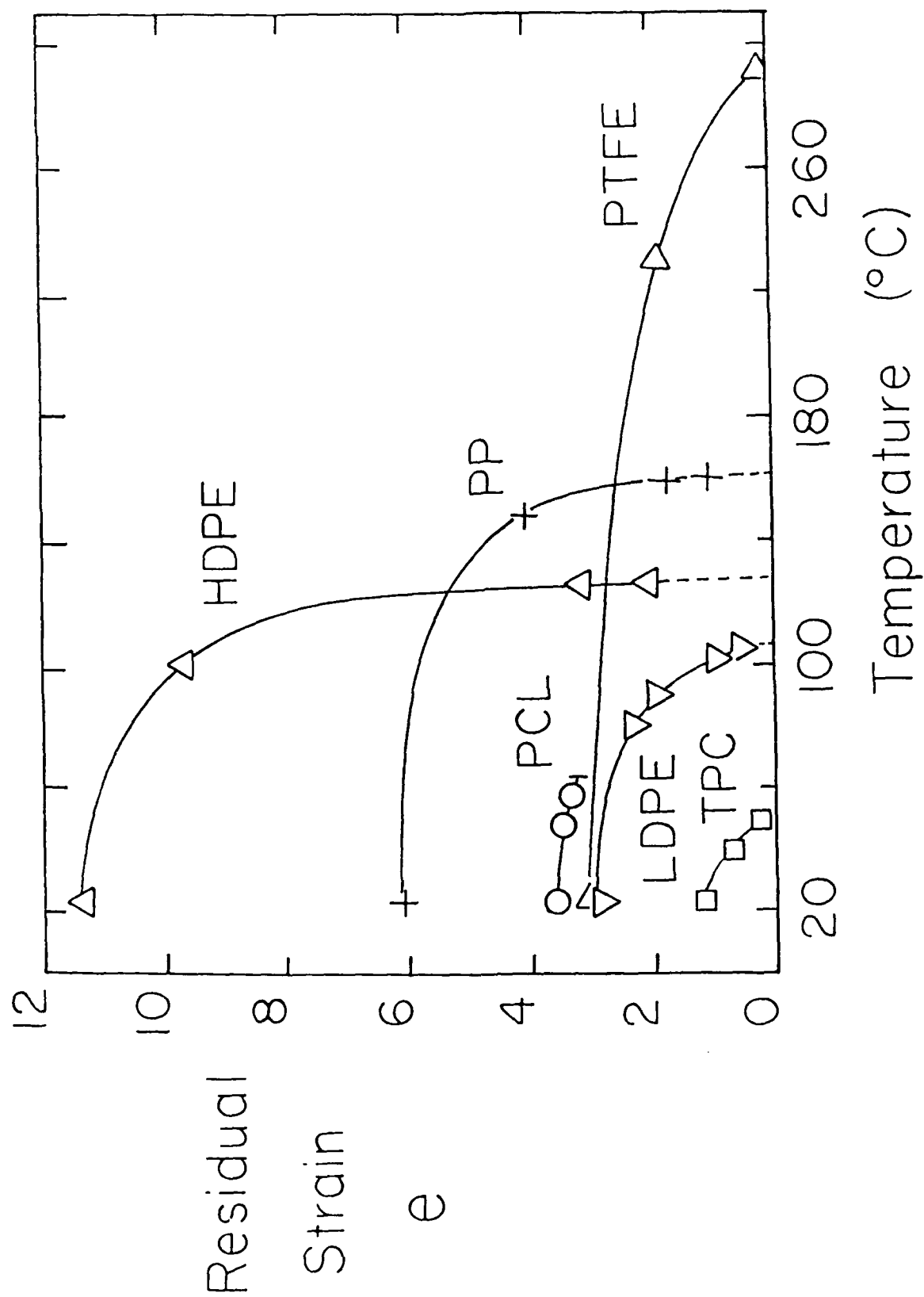


Figure 6

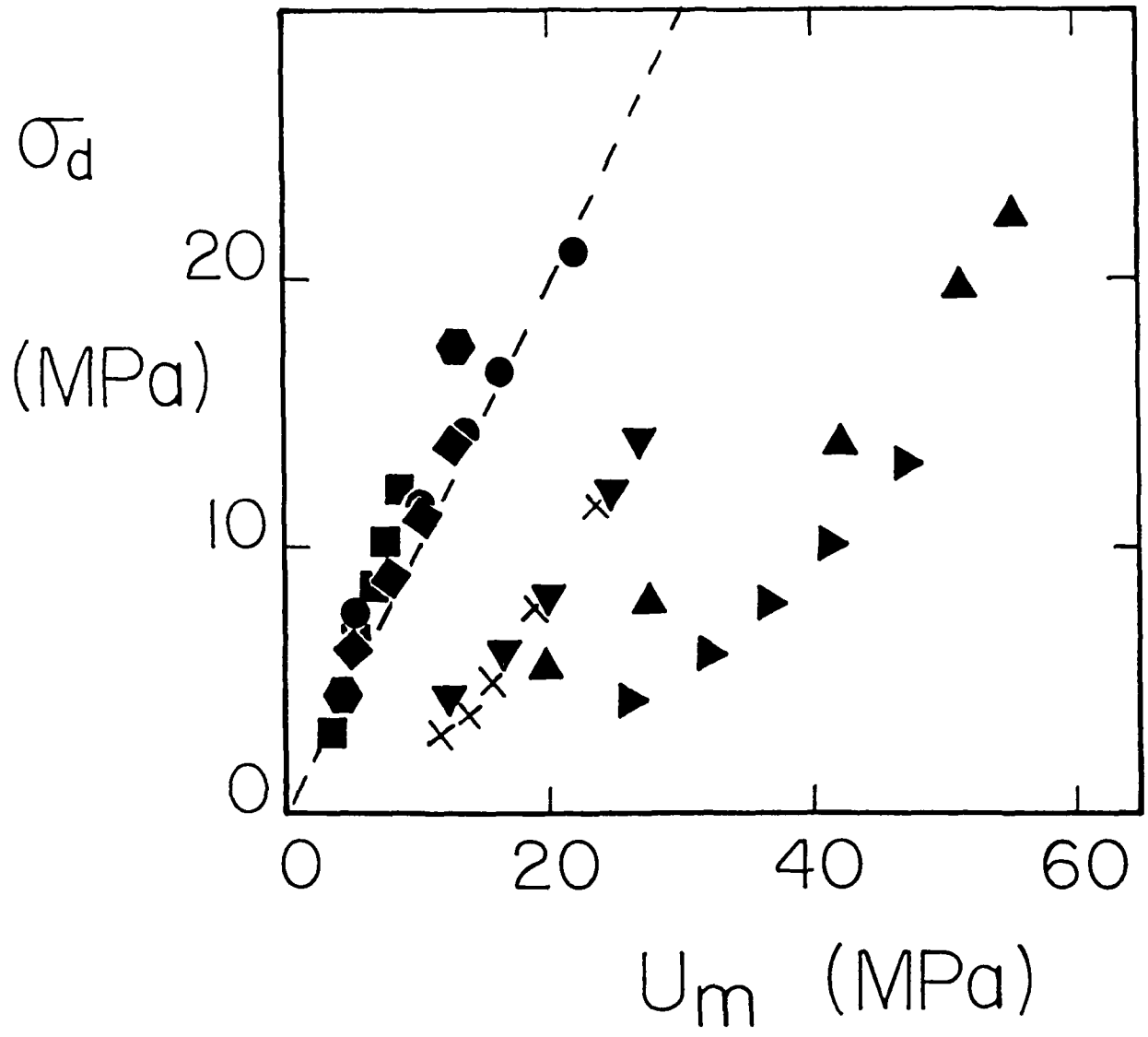
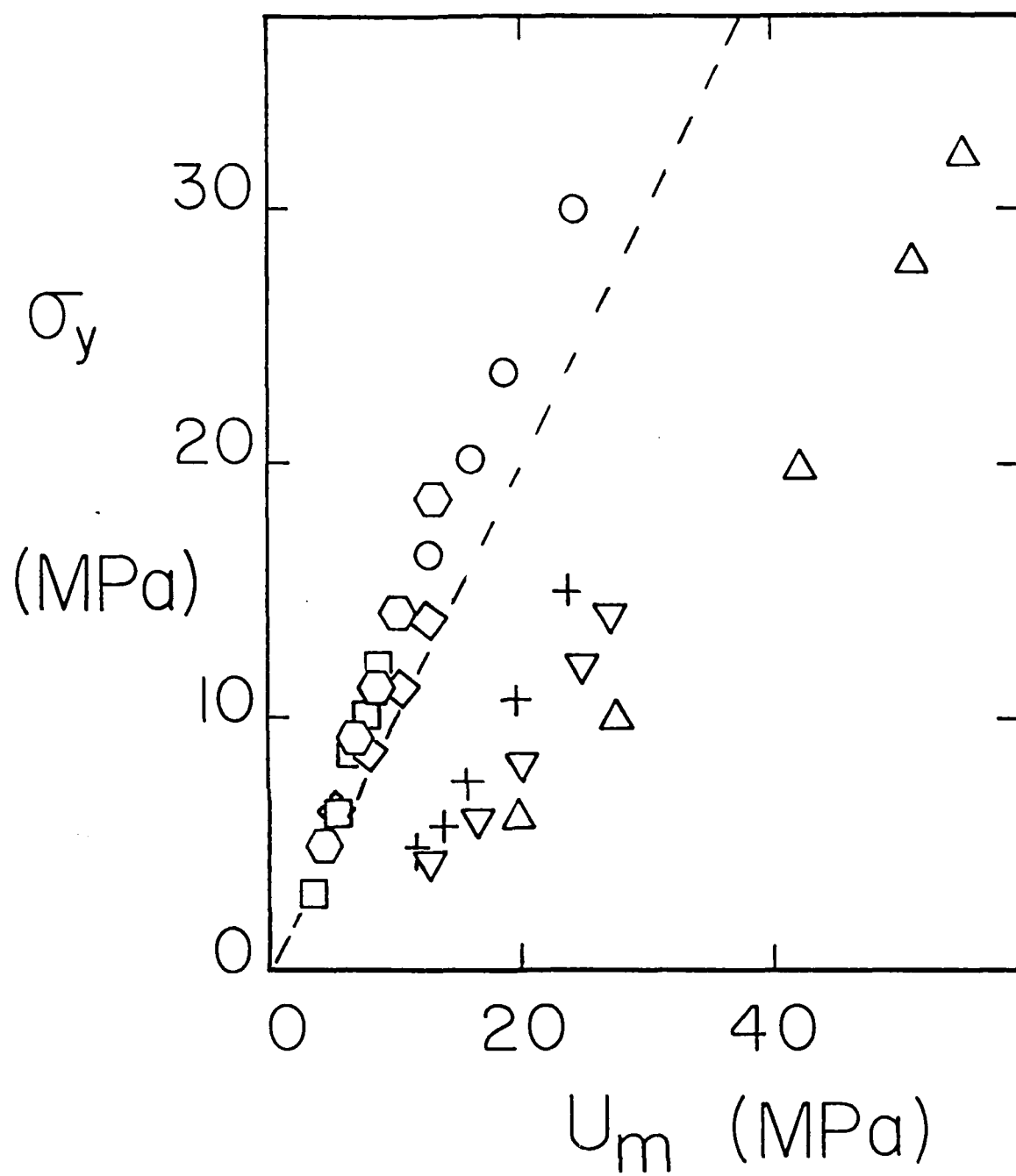


Figure 7



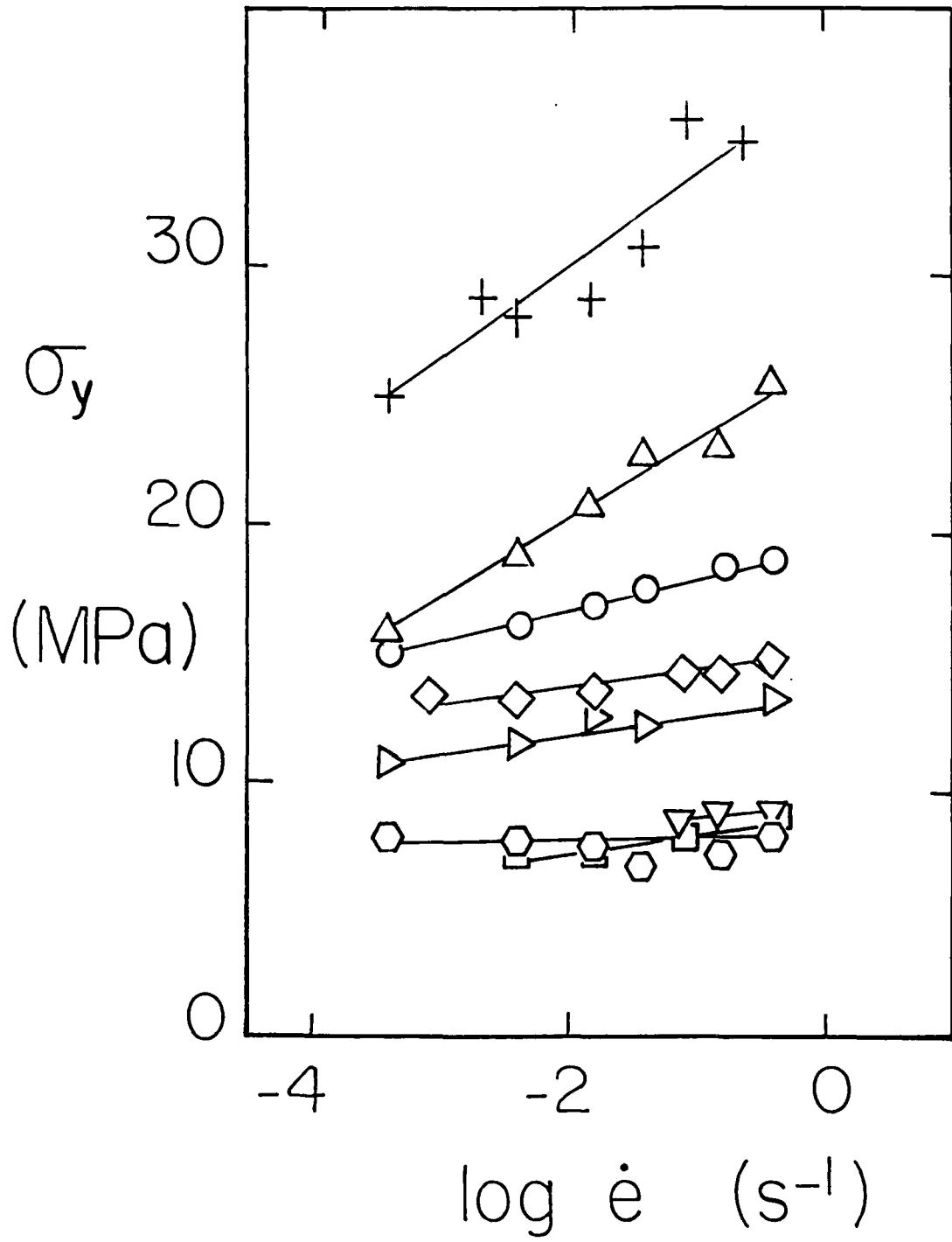


Figure 9



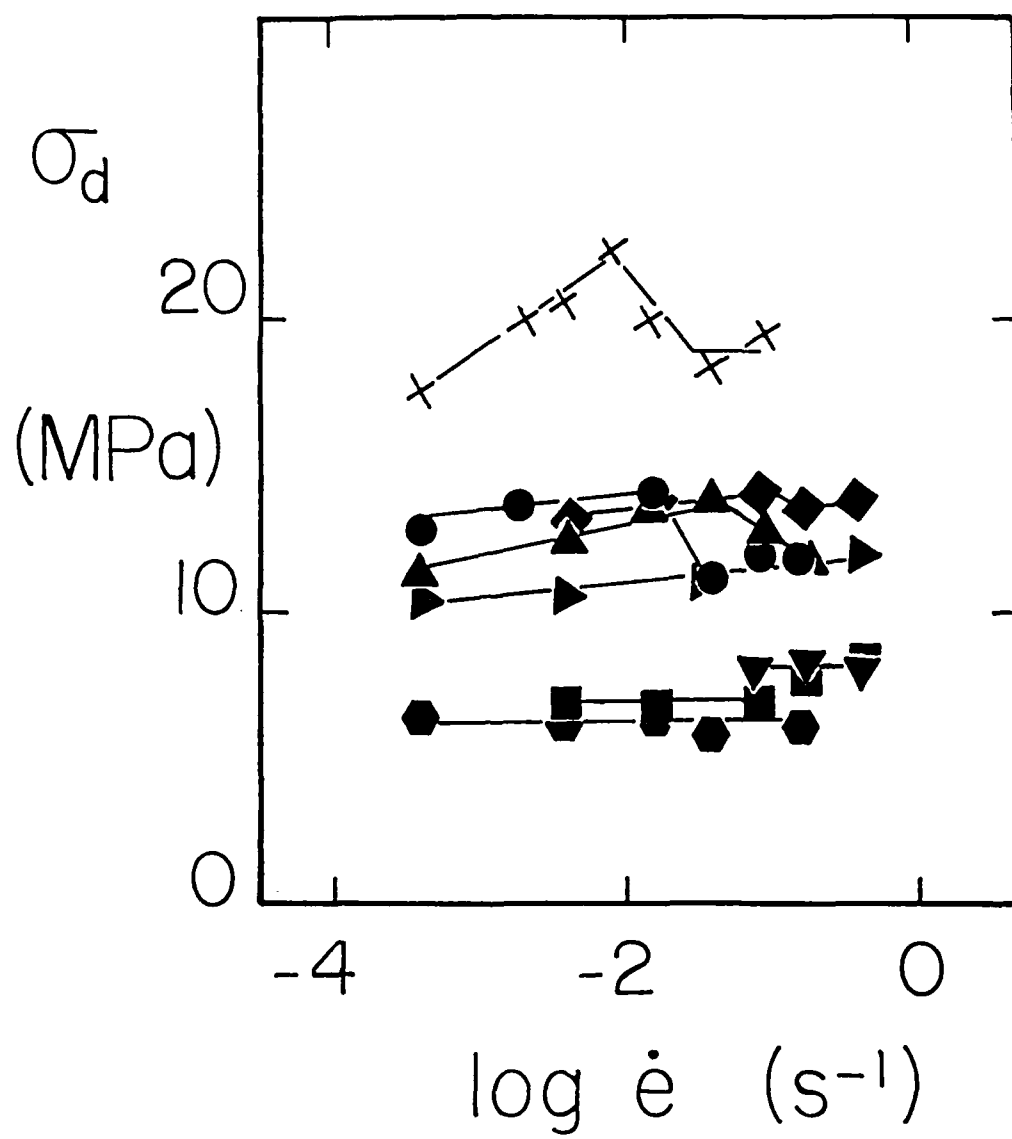


Figure 10

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